

# Systematic variation in North American tree species abundance distributions along macroecological climatic gradients

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**Systematic variation in North American tree species abundance distributions along macroecological climatic gradients**

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**DATA AVAILABILITY**

Our analyses were based on publicly available plot-level data produced by the United States Department of Agriculture, Forest Service's Forest Inventory and Analysis Program (<http://fia.fs.fed.us/>).

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Francois Rigal provided advice on spatial logistic regression. This is paper number 33 of the Birmingham Institute of Forest Research.

## AUTHOR CONTRIBUTIONS

T.J.M. designed the study; C.W.W. and T.A.M.P. provided data; T.J.M. ran the analyses; T.J.M. wrote the manuscript with the help of J.P.S.; all authors commented on the manuscript.

## BIOSKETCH

**Tom Matthews** is a Research Fellow at the University of Birmingham, UK. His research interests span community ecology, macroecology and biogeography. He is particularly focused on investigating global environmental change questions using macroecological methods and theory.

## Abstract

**Aims:** The species abundance distribution (SAD) is a fundamental pattern in macroecology. Understanding how SADs vary spatially, and identifying the variables that drive any change is important from a theoretical perspective as it enables greater understanding of what factors underpin the relative abundance of species. However, precise knowledge on how the form of SADs varies across large (continental) scales is limited. Here, we use the shape parameter of the gambin distribution to assess how meta-community scale SAD shape varies spatially as a function of various climatic variables and dataset characteristics.

**Location:** Eastern North America.

**Time period:** Present Day.

**Major taxa studied:** Trees.

**Methods:** Using an extensive continental scale dataset of 863,930 individual trees in plots across Eastern North America (ENA) sampled using a standardised method, we use a spatial regression framework to examine the effect of temperature and precipitation on the form of the SAD. We also assess whether the prevalence of multimodality in the SAD varies spatially across ENA as a function of temperature and precipitation, as well as other sample characteristics.

**Results:** We found that temperature, precipitation and species richness can explain two thirds of the variation in tree SAD form across ENA. Temperature had the largest effect on SAD shape, and it was found that increasing temperature resulted in more log-series like SAD shapes (i.e. SADs with a relatively higher proportion of rarer species). We also found spatial variation in SAD multimodality as a function of temperature and species richness.

**Main conclusions:** Our results indicate that temperature is a key environmental driver governing the form of ENA tree meta-community scale SADs. This finding has implications for our understanding of local-scale variation in tree abundance, and also suggests that niche factors and environmental filtering are important in the structuring of ENA tree communities at larger-scales.

## INTRODUCTION

The species abundance distribution (SAD) describes how the number of individuals is distributed across all species in a sample or community, and is one of the fundamental patterns in macroecology (May, 1975; Gaston & Blackburn, 2000; McGill et al., 2007; McGill, 2011). Whilst a multitude of different SAD models have been proposed (see McGill et al. 2007), SADs can be grouped into two main classes: logseries and lognormal-like shaped distributions (Ulrich, Olrik, & Ugland, 2010; Ulrich, Kusumoto, Shiono, & Kubota, 2016). The logseries distribution itself results from the Poisson sampling of a gamma distribution after a certain relevant limit is taken, and it is characterised by a right-hand skewed curve with a modal value of one (Fisher, Corbet, & Williams, 1943). The lognormal distribution represents a situation in which the logarithms of abundances follow a Gaussian distribution and it is characterised by a community in which species of intermediate abundance are most prevalent (Preston, 1948; May, 1975). Both the logseries and lognormal are unimodal models, which have been the focus of many studies until recently (but see Ugland & Gray, 1982). However, recent work has indicated that a small proportion of empirical SADs are in fact multimodal (e.g. Dornelas & Connolly, 2008; Vergnon, van Nes, & Scheffer, 2012; Matthews & Whittaker, 2015; Antão, Connolly, Magurran, Soares, & Dornelas, 2017). For example, a recent synthesis of 117 datasets found significant evidence of multimodality in approximately 20% of cases (Antão et al., 2017). A number of potential causes of multimodality in SADs have been put forward, such as the amalgamation of different types of species within a single sample (e.g. core and satellite species; Magurran & Henderson, 2003; Matthews & Whittaker, 2015), and the increasing taxonomic breadth, sampling variation, and spatial extent (i.e. increasing ecological heterogeneity; Antão et al. 2017) of a study. However, variation in the prevalence of SAD multimodality at large scales and across ecological gradients is largely unknown.

Whilst a large proportion of previous (unimodal) SAD studies has focused on either finding the best fitting model given a set of local-scale ecological data (e.g. Ulrich et al., 2010), or using the SAD to test the performance of a particular theory or model (e.g. Volkov, Banavar, Hubbell, & Maritan, 2003), there has been increasing recognition of the importance of assessing how different SAD properties change across ecological gradients, such as climate, succession and disturbance gradients (e.g. Dornelas, Soykan, & Ugland, 2011; Matthews et al., 2014; Ulrich et al. 2016; Matthews, Borges, de Azevedo, & Whittaker, 2017). Traditionally, these SAD gradient studies have mostly been undertaken at relatively local scales (e.g. Bazzaz, 1975; Matthews et al., 2014). However, likely due to the increased availability of open source SAD datasets, in combination with an increase in computer processing power, there has been a rise in the number of SAD studies focusing on larger, macroecological, scales (e.g. Ulrich et al. 2010, 2016; White, Thibault, & Xiao, 2012; Kubota, Kusumoto, Shiono, Ulrich, & Jabot, 2015). Generally speaking, macroecological scale analyses are characterised by a trade-off between global coverage and local/regional resolution, that is, studies that analyse datasets from across multiple continents (e.g. Ulrich et al., 2016) tend not have very high coverage in any particular region / continent, and *vice versa*. Thus, most global scale SAD analyses have large gaps within any given region. Whilst this is not a criticism of global SAD analyses, which are often able to identify broad scale patterns, it often involves analysing datasets from multiple studies that employ different sampling methods and have varying aims, which may result in some patterns of interest being

obscured. A different and more effective approach involves extensively sampling one large region using a standardised sampling protocol. This approach is arguably better at identifying spatial variation in SAD properties as it allows for more variables to be controlled, but, due to the resources required to undertake the standardised sampling, has been employed less frequently in SAD studies (but see White et al., 2012, Locey & White, 2013).

Understanding how SADs vary spatially is important from a theoretical perspective as it enables greater understanding of: (1) what underpins the relative abundance of species (MacArthur, 1960, 1972; May, 1975; Matthews et al., 2017), and (2) large-scale species richness gradients (Rosenzweig, 1995; Currie et al., 2004). However, precise knowledge on how the form of SADs varies across large scales, and the role of different processes driving this change, is limited (Ulrich et al., 2016). It can be theorised that variation in climate across space will be important in driving variation in SAD form. Climatic variables are known to be important drivers of species richness gradients at macroecological scales (Currie & Paquin, 1987; Brown et al., 2004; Field et al., 2008). In particular, temperature and precipitation are known to be the primary limiting drivers of richness variation in North American trees (Currie & Paquin, 1987; Allen, Brown, & Gillooly, 2002; Whittaker, Willis & Field, 2003). The effect of variation in climate on the shape of the SAD is largely unknown, but based on the findings of previous studies on species richness gradients (e.g. Currie & Paquin, 1987; Currie et al., 2004), we predict logseries SAD shapes to be more prevalent with increasing temperature and precipitation. Primary productivity correlates strongly with climatic variables, and higher energy and productivity is known to: (1) result in finer scale divisions of niche space (Whittaker et al., 2003), and (2) enable areas to support more individuals (Currie et al., 2004) at smaller minimum viable population sizes (Hawkins et al., 2003). In addition, it has been argued that, in contrast to the theoretical predictions of the species-energy hypothesis, populations of species are smaller in more productive environments (Currie et al., 2004). These factors have been postulated to result in greater richness in productive environments, but together would also mean a higher proportion of rarer species and thus logseries SAD shapes. The role of climatic variables in driving multimodality in SADs has not, to our knowledge, been previously assessed at this scale.

Macroecological SAD studies have tended to compare the fit of different models, and then assessed spatial variation in the best fitting model (e.g. Ulrich et al., 2016). However, this approach does not necessarily provide accurate information about the shape of the SAD, as certain SAD models are relatively flexible and can fit a range of SAD forms, and choosing a best fitting model does not necessarily mean that it fits the data well (i.e. none of the models in the comparison may provide an accurate representation of the SAD shape). An alternative approach focuses on a single value that characterises the shape of the SAD (Ulrich, Nakadai, Matthews, & Kubota, 2018), such as the shape parameter of the gambin model (Ugland et al., 2007). Gambin is a stochastic model which combines the gamma distribution with a binomial sampling method; the unimodal gambin model has a single free parameter ( $\alpha$ ), which characterises the distribution shape: low values indicate logseries shaped curves, whilst higher values indicate more lognormal shaped curves (see Fig. 1 for an example). Gambin has been shown to provide good fits to a wide variety of empirical datasets, and  $\alpha$  has been found to represent a useful metric that can be used to assess the effect of different variables on SAD shapes (Dornelas et al., 2011; Matthews et al., 2014; Arellano et al., 2017). Recent methodological developments (Matthews et al., 2018) have derived the likelihood functions

for multimodal gambin models (multimodality also being a measure of the shape of the SAD), thus providing a means of easily assessing multimodality in SAD datasets.

Here, we analyse an extensive dataset of 863,930 individual trees in 33,282 plots across Eastern North America (hereafter, ENA) sampled using a standardised method, to examine the effect of climate on the form of ENA tree SADs across broad spatial scales. We combined adjacent plots (within grid squares of roughly 44km by 44km) to create coarse-scale SADs; thus, we are analysing SADs at the meta-community scale. We use gambin's  $\alpha$  to assess how SAD shape varies spatially as a function of various climatic variables and dataset characteristics. We hypothesise that, due to the arguments outlined above, we will observe a shift from lognormal to logseries shaped SADs with increasing temperature and precipitation. We also assessed the prevalence of SAD multimodality and whether SAD multimodality varies spatially as a function of temperature and precipitation.

## **MATERIALS AND METHODS**

### ***Data and sampling methodology***

Our analyses were based on publicly available plot-level data produced by the United States Department of Agriculture, Forest Service's Forest Inventory and Analysis Program (FIA; <http://fia.fs.fed.us/>). The FIA program conducts a systematic and consistent inventory of all forest land in the United States, with a comprehensive summary of the associated data and sampling methodology provided by O'Connell et al. (2017). Briefly, inventory plots are systematically distributed across the entire United States with remotely sensed information used to identify plots that are located in a forest land use where a field plot is measured for site/forest attributes. Each FIA plot comprises four circular subplots of area 0.017 ha, each located within a circular 0.10 ha macroplot. All free-standing woody stems (live and dead) with a diameter  $\geq 12.7$  cm are sampled within each subplot. Within each subplot there is a circular 0.001 ha microplot in which all live stems with a diameter  $\geq 2.54$  cm are sampled (O'Connell et al., 2017). The full dataset contained sampling data from two time periods, that is, each plot was re-sampled a second time on average five years later. For this study, we only used the data from the first sampling period. The location of the plots is illustrated in Fig. 2.

Annual mean temperature and annual mean precipitation data for each plot were sourced from the WorldClim database (Version 2.0; 2.5-minute resolution; Fick & Hijmans, 2017) using averages based on annual means (1970-2000) and extracted using the 'raster' R package (Hijmans, 2017; see Appendix S1 for further details). Climatic seasonality variables were also extracted but not used further due to multicollinearity issues (based on variance inflation factors).

### ***Dataset format and fitting the gambin model***

Whilst the full dataset had a very high spatial resolution (i.e. coverage of plots within ENA), the individual plots did not contain sufficient individuals to confidently fit SAD models (see McGill, 2011). Thus, we pooled all plots within a given distance to create meta-community scale SADs. To achieve this, we divided the ENA into a grid of squares of  $x_1$  by  $x_2$ . For each grid square, we then pooled all plots with centre points within the boundaries; thus, creating individual meta-community samples of individuals (hereafter, 'samples') for each grid square. For the main analyses, we used 0.4 degrees of latitude (i.e.  $x_1 = 0.4$  degrees). As the length of a degree of longitude varies with latitude, we varied the selected degrees of

longitude ( $x_2$ ) at different latitudinal bands to ensure the grid squares were all approximately the same size (roughly 44km by 44km).

As SAD model parameters are known to be biased when sample size is small (McGill, 2011; Matthews et al., 2014), we removed all samples with less than 500 individuals. For the remaining samples, we fitted the one-component (unimodal) gambin model to each sample using the gambin R package (version 2.4, Matthews et al., 2014). Because SAD model parameters are sensitive to variations in sample size (McGill, 2011), we used a procedure where, for each sample, we subsampled 500 individuals, fitted the unimodal gambin model to this subsample and stored the  $\alpha$  parameter value. As this subsampling procedure is stochastic, we repeated the process 100 times for each sample and took the mean  $\alpha$  value. The 100 subsamples were also used to create estimates of the standard error of the mean value. As comparing SAD model parameters only makes sense if the model provides a reasonable fit to the data, for each model we fitted we also stored the  $X^2$  goodness of fit statistic and its associated  $P$ -value; the mean values of the 100 subsamples were then calculated. We then discarded all samples where the mean  $P$ -value was less than 0.05. Occasionally, the model did not fully converge and the fit generated unrealistically high values of  $\alpha$  (e.g. 50). Following previous work and earlier versions of the gambin package (Matthews et al., 2014) we discarded all samples that had a mean  $\alpha$  value  $> 15$ . Species identities were taken from O'Connell et al. (2017; see their Appendix F).

### ***Spatial regression analyses***

To determine whether temperature and precipitation could explain any of the variation in SAD form across our samples, we used a spatial linear regression modelling approach. For the response variable, we used the  $\alpha$  values from the fits of the unimodal gambin model to the samples. The distribution of  $\alpha$  values was skewed, so it was log transformed to enable use of standard Gaussian linear models. We included three predictor variables (temperature, precipitation and species richness of the sample) and all predictor variables were standardised to have a mean of 0 and a standard deviation of 1 to enable comparison of effect sizes. Species richness was simply the number of species in a sample, whilst precipitation and temperature were taken as the mean values of the plots within a sample. The variance inflation factors of all predictors were below three. The number of individuals was not included as a predictor as this was standardised prior to fitting the gambin models. First, we fitted a standard linear model using all predictors. We tested for spatial autocorrelation in the residuals of this model fit using a permutation test (999 permutations) for Moran's I statistic and the 'spdep' R package (Bivand, 2017); spatial weights for neighbour lists were calculated using the 'knearneigh' ( $k = 4$ ) and 'nb2listw' functions and row standardised weights. This test revealed strong spatial autocorrelation in the residuals (Moran's  $I = 0.38$ ,  $P = 0.001$ ). To account for this, we used a spatial regression framework (Ward & Gleditsch, 2008; Bivand, 2017). We fitted both a spatial lag model (i.e. a spatial simultaneous autoregressive lag model) and a spatial error model (i.e. a spatial simultaneous autoregressive error model) using the 'spdep' R package and compared the models using Akaike's information criterion (AIC). Due to the large number of data points, it was not necessary to use  $AIC_c$ . Using the best-fitting spatial regression model, we fitted the global model (i.e. with all predictors), and models with all possible predictor combinations that included species richness; species richness was included in all models as it was a predictor we wanted to control for. We also fitted a null model (just an intercept term, Mac Nally et al., 2018). Model comparisons used

an information theoretic approach (Burnham & Anderson, 2002). All global and best-fit models were re-checked for residual spatial autocorrelation and we also calculated Nagelkerke's pseudo  $R^2$  values to assess model fit. To validate models, we extracted the fitted values and the residuals from the spatial error model fit object, and constructed qqplots to check for residual normality and plotted the fitted values against the residuals to check for homoscedasticity. We constructed partial regression plots to assess the effect of each variable after taking into account the effect of the other predictors.

### ***Assessing multimodality using multiple-component gambin models***

To assess whether the prevalence of multimodality in the SAD varied as a function of the predictor variables, for each sample (from the 0.4 degrees of latitude grid) we fitted both the one-component and two-component gambin models using the gambin R package (version 2.4; Matthews et al., 2018) and derived the Bayesian information criterion (BIC) values. We used BIC here rather than AIC as the former is known to more strictly penalise more complex models than AIC (Burnham & Anderson, 2004), and this is a desirable property in this context as arguably a test of multimodality should be conservative. The two-component model was considered the best fit model if it had a  $\Delta$ BIC value lower than the one-component model (Burnham & Anderson, 2002, 2004). As we were not interested in comparing parameter values across samples in this part of the analysis, we fitted the models without standardising for the number of individuals in the samples. We excluded all samples where neither the one-component or two-component model had a  $X^2$   $P$ -value greater than 0.05. We converted the number of times the two-component model was the best fit model into a binomial variable to be used as a response variable in a binomial GLM using temperature and precipitation as predictor variables. As we did not standardise by sample size, we also included the number of individuals and number of species in a sample as predictors. All predictors were standardised to have a mean of zero and a standard deviation of one. The variance inflation factors of all parameters were below five. To deal with spatial autocorrelation, we created an autocovariate to be used in autologistic regression, using the 'autocov\_dist' function (type = "inverse", style = "W") in the spdep R package. We set the neighbourhood radius to 50 km to ensure there were few regions that included points with zero links to other points (0.04 % of regions, average number of links = 2.61). We used the MuMIn R package (Bartoń, 2012) to fit a complete set of models considering all predictors; the autocovariate was set as fixed. As with the unimodal model selection analysis, we used AIC to compare regression models. Weight of evidence (WoE) values for each predictor variable were calculated by summing the AIC weights for all models in which a variable was present (Burnham & Anderson, 2002; Giam & Olden, 2016). McFadden's pseudo  $R^2$  was calculated for each model using the formula:  $1 - (\text{residual deviance} / \text{null deviance})$ .

### ***Sensitivity analyses***

In order to determine whether our results were influenced by the location and size of the grid squares, the pooling of data within grid squares in general, and to test the effect of potentially including managed plots on our results, we ran a number of sensitivity analyses to account for these factors (the full methods are provided in Appendix S1).

Inspection of plots of the standard error of the mean alpha values (the mean of the alpha values from the 100 subsamples) indicated that the standard error increased with increasing mean alpha (Figure S1 in Appendix S2). Thus, to ensure that this did not bias our results we:



1) re-ran the main analyses using unstandardized alpha values (i.e. the gambin model was fitted without any subsampling), and 2) we used the standard errors as weights in a linear regression model selection. The standard errors were normalised between 0 and 1 and we used the inverse of these values as the weights. It was necessary to use a standard linear model as it was not possible to add weights to our spatial regression models. Re-running the analyses using unstandardized alpha values also enabled us to check that our random subsampling did not affect the results. For example, this could happen as our subsampling procedure randomly sampled individuals from a plot, which disregards the possibility that individuals of a species are spatially aggregated rather than randomly distributed within a plot.

In addition, when the number of species in a sample is low, the shape of the SAD is constrained (Locey & White, 2013). Thus, to test whether our results are simply an artefact of low richness in certain samples we ran an additional simulation analysis where we assessed the effect of the number of species in a sample on the alpha value of the unimodal gambin model (full details in Appendix S1).

All analyses were undertaken in R (version 3.5.1; R Core, Team 2017). The R code is provided in an online repository on GitHub (txm676/NEA\_SADs).

## RESULTS

Across the 33,282 plots there were 863,930 individual trees representing 214 species. Using a ca. 44km by 44km grid square and a minimum number of individuals threshold of 500, there were 763 coarse-scale SAD samples. After removing samples to which the one-component gambin model did not provide a good fit (according to the  $X^2$  statistic or an unreasonably high  $\alpha$  value), we were left with 737 samples distributed across ENA. The mean species richness of the samples was 30 (SD = 8), whilst the mean number of individuals was 904 (SD = 343, although the number of individuals in each sample was standardised prior to model fitting).

### *Variation in gambin's alpha along macroecological gradients*

When all predictors were considered, the spatial error model (AIC = 644.8) had a lower AIC value than the spatial lag model (AIC = 647.8) and the standard non-spatial linear model (AIC = 822.8), and the residuals were no longer autocorrelated (Moran's I of the global model = -0.03,  $P = 0.91$ ). Thus, the spatial error model was used in subsequent analyses.

There was substantial spatial variation in  $\alpha$  (see Fig. 2). The best spatial error model (i.e. the model with the lowest AIC) contained temperature and species richness (Table 1); temperature had the largest effect on  $\alpha$  (i.e. this variable had the largest coefficient), followed by species richness. A second model containing all three predictors was also within 2  $\Delta$ AIC values of the global model (Table 1). The model with the lowest AIC value explained a large amount of the variance in SAD form (pseudo  $R^2 = 0.65$ ). The  $\Delta$ AIC value of the null model was 132.5 (Table 1), meaning the best model provided a substantially better fit than an intercept only model. The partial regression plots (Fig. 3) of the global model (i.e. the model with all three predictors) show a stronger negative effect of temperature on  $\alpha$  (Fig. 3a) relative to the effects of species richness (Fig. 3c) and precipitation (Fig. 3b). The residuals of the best spatial error model were not significantly autocorrelated (Moran's I = -0.03,  $P =$

0.91) and were observed to be normally distributed according to both the qqplot and histogram (Shapiro-Wilk normality test on the residuals:  $w = 1.00$ ,  $P = 0.15$ ).

### ***Multimodal model results***

After filtering out samples according to our acceptance criteria (i.e. number of individuals and  $X^2$  goodness of fit test), we were left with 653 samples. Across these, the two-component (bimodal) gambin model had the lowest BIC value in 65 cases (10%). Examples of unimodal and bimodal SADs are provided in Fig. 4a,b. A heat map of the bimodal BIC weights is provided as Fig. S2 in Appendix S2. The best binomial GLM model contained temperature, number of species and number of individuals, in addition to the spatial autocovariate (Table 2). The pseudo- $R^2$  of the best model was low (0.09) and there was no residual spatial autocorrelation (Moran's  $I = 0.03$ ,  $P = 0.10$ ). There were two additional models with  $\Delta AIC$  values less than two; temperature and species richness were included in both (Table 2). Temperature had a WoE value of one, whilst precipitation, and the number of individuals and species had values of 0.34, 0.60 and 0.98, respectively (Table 2). The fit of a simple non-spatial logistic regression model using just temperature as a predictor is shown in Fig. 4c; it shows an increasing probability of a one-component model providing the best fit with increasing temperature.

### ***Sensitivity analyses***

Removing the potentially managed plots, re-running the analyses from different starting points to create the grid cells, or with smaller grid squares did not affect the overall results: the spatial model selection results, partial regression plots, and binomial GLM model selection analyses produced largely similar outcomes (see Appendix S2). The main difference was the performance of the precipitation variable, which had a positive effect in some of the smaller grid square models (in both the unimodal and multimodal model selection analyses) and in two of the shifted grid square analyses (Appendix S2).

Re-running the spatial error model selection using alpha values generated from fitting gambin to the raw plot data also did not affect the overall results. Regardless of the number of individuals threshold used (i.e. 25 or 50; which resulted in 10,181 and 729 plots, respectively), the model selection results were very similar (Tables S6 & S7 in Appendix S2). Again, the main difference was the performance of the precipitation variable, which was included in the best model and had a positive effect, in both cases. Re-running the spatial error model selection using unstandardized alpha values did not change the overall results (Table S8 & Figure S5 in Appendix S2). In addition, using the standard error (of mean alpha) values as weights in a standard linear model resulted in a very similar global model (Table S9 in Appendix S2).

The species richness simulations indicated that the alpha parameter of a sample is an accurate estimate of the population alpha value when the number of species is greater than ten (see Figure S6 in Appendix S2). When the number of species is less than 10, the alpha value tends to be inflated. As only one of our samples in the main analysis had fewer species than ten (nine), we are confident that our results are not an artefact of low richness in our samples.

## DISCUSSION

The majority of SAD analyses are undertaken at local scales, and thus less is known about SADs at larger meta-community scales. In addition, the use of standardised plot data avoids the biases introduced in many macroecological studies whereby data from multiple studies that use different sampling methods, are combined. We found that our global model (the two climatic variables and species richness) can explain around two thirds of the variation in meta-community SAD shape across ENA. This is a significant amount; a recent global synthetic analysis (i.e. combining multiple independent studies) of SADs was able to explain roughly 20% of variation in SAD form (Ulrich et al., 2016). We also found some spatial variation in SAD multimodality as a function of temperature, species richness and, to a lesser extent, the number of individuals.

Model selection indicated that temperature was the most important variable driving variation in  $\alpha$ ; it had the largest effect in all  $\Delta AIC < 2$  models (Table 1). Our findings show that, in line with our prediction, the effect of temperature was negative (see Fig. 3); increasing temperature resulted in lower  $\alpha$  and thus more logseries-like SADs. This finding suggests that temperature is more important than water in structuring ENA tree SADs. Allen et al. (2002) report a similar finding for the species richness of North American trees. However, although precipitation had a smaller effect than temperature, it was still retained in a model with  $\Delta AIC < 2$ . It is likely that at some extremes, precipitation has a greater effect on SAD form (e.g. highly arid areas), and that our dataset did not cover enough of these extreme environments (see also Hawkins et al., 2003). It is also possible that other variables (e.g. potential evapotranspiration, Currie et al., 2004) might be more accurate measures of water availability and water deficit than mean precipitation (Anderegg et al., 2015). A more in-depth analysis of the role of different productivity metrics on SAD form would be an interesting future step, although such an analysis is reliant on the availability of suitable data at large scales. It should be noted that in some of the sensitivity tests the effect of precipitation on  $\alpha$  was positive (rather than negative as in the main analysis; compare for example Fig.3 with Fig.S4 in Appendix S2). However, the effect was often close to zero and the standard error of the effect often overlapped zero (e.g. see Table S3 in Appendix S2). In addition, within the same model selection analysis (e.g. Table S3 and S7 in Appendix S2) the effect of precipitation on  $\alpha$  was found to switch between positive and negative for different models. Thus, the effect of precipitation on  $\alpha$ , based on these data at least, can be considered negligible.

The strong role of temperature and thus energy availability implies that niche processes (e.g. niche division) leave an imprint on the SAD. Previous climate-richness gradient studies have shown that diversity is positively correlated with productivity, due in part to the fact that more individuals can be supported in productive ecosystems and the minimum viable population sizes of individual species are often smaller; thus, a larger number of species, with smaller population sizes, can be supported in a given unit of area than in less productive systems (Allen et al., 2002; Hawkins et al., 2003; Brown et al., 2004). For example, the average population densities and population sizes of tree species have both been shown to decrease with increasing temperature (Allen et al., 2002) and decreasing latitude (Currie et al., 2004). A separate but linked idea is the theory that greater niche division in more productive environments enables more species to coexist in a given area (Rosenzweig, 1995; Whittaker et al., 2003). If abundance is linked to niche size (MacArthur, 1972), then greater niche division would result in a higher proportion of relatively rare species being found in

more productive environments, which would also explain our findings. The negative effect of species richness on  $\alpha$ , whilst less than the effect of temperature (Table 1), also fits into this rationale: more productive environments, in general, support larger numbers of species (Hawkins et al., 2003). A novel finding of our study is that abundance is distributed across these larger number of species in a less even way than in cooler environments. These observations could also be due to the filtering out of rarer species (i.e. species with small populations) in colder regions, which in turn could be linked to tropical niche conservatism (Wiens et al., 2010); fewer lineages are adapted to colder temperatures, and thus there is less competition and a larger proportion of species is able to have higher relative abundance. Another possibility is that increasing temperature results in a higher rate of speciation (Allen, Gillooly, Savage, & Brown, 2006), leading to a larger number of young species with relatively small population sizes and thus more log-series like SADs. These different explanations are not necessarily mutually exclusive.

An alternative explanation is the possible constraining influence of community richness on the shape of the SAD (Locey & White, 2013). A meta-analysis by White et al., (2012), who included in their analysis a subset of the plots we have analysed, has shown that the maximum entropy theory of ecology (see Harte, 2011) can successfully capture a large proportion of the variation in SADs. In addition, Locey & White (2013) found that the form of SADs in many cases is not different to the central tendency of the feasible set of possible distributions. However, our results are not actually in contradiction with those of White et al. (2012) or Locey & White (2013). Both these studies found that the application of a maximum entropy model and the feasible set framework to empirical data does not capture all of the variation in SAD form, particularly in cases where the SAD is exceptionally even or uneven (see Locey & White, 2013). More importantly, as the authors state, the results of these studies do not imply that ecological processes are unimportant. Rather, ecological processes are likely to be important indirectly through their impacts on the state variables and constraints considered (e.g. the total number of individuals or the number of species, see Harte, 2011). Our results, alongside the many studies of large-scale richness gradients (e.g. Currie & Paquin, 1987; Hawkins et al., 2003; Field et al., 2008), indicate that temperature in particular is a key variable of interest in this regard.

Whilst the unimodal gambin model provided a better fit, according to BIC, in the majority of cases, the bimodal model was the best fit model to a small proportion of samples (10%). Multimodality is also a measure of the shape of a SAD, and our multimodal SAD model selection results (Table 2) provide further evidence in support of the role of temperature in driving variation in SAD shape. However, it should be noted that the amount of variation explained by the best model in this case (pseudo  $R^2 = 0.09$ ) was much lower than in the unimodal gambin alpha analyses (Table 2) and it is thus hard to make any general conclusions on the variables driving this pattern. That being said, one interesting result is that the effect of temperature and species richness (in the models in which species richness was included, see Table 2) have opposite signs; temperature has a negative effect (see Fig.4c), and species richness a positive effect, on the log odds prevalence of bimodality in the analysed SADs (Table 2). The reasons for contrasting effects of temperature and richness are unclear. One potential explanation might be that an additional variable not included in our analysis covaries with either or both temperature and species richness, such as topographical relief or human disturbance. Another potential explanation for the presence of multimodal SADs more

generally is the possible presence of strong fine-scale climatic gradients within some of our coarse-scale grid squares; the fact that our sensitivity analysis using a smaller grid square size provided evidence for a relatively larger (compared to the larger grid square analysis) positive effect of precipitation on the prevalence of multimodality provides evidence supporting this explanation. Further work is needed to explore these possibilities, and to identify additional covariates that explain more variation than those analysed here.

Forest management provides another potential confounding factor in our interpretation. Due to the systematic nature of the FIA inventory, some of the plots included in the study dataset were in managed forest (see O'Connell et al., 2017). The inclusion of these forests could potentially have biased our results if there is strong spatial variation in the location of managed forest plots in relation to the other covariates. For example, there are currently known to be large tracts of managed forests (e.g. aspen and birch, and spruce and fir plantations) in northern USA. However, whilst management was not explicitly recorded during sampling, each of the plots (and individual trees) included in our analysis have been surveyed at multiple points in time, and when an individual tree was found to have died between time periods a cause of death was inferred. This allowed us to remove all plots that contained several trees that were listed as having died due to management related activities and re-run the analyses (which did not affect the overall results; see Appendix S2). Whilst this is not a perfect metric of management and human disturbance, we are confident that our overall results are not simply an artefact due to the inclusion of managed forests.

In a previous study of the SADs of North American trees using a functional trait-based maximum entropy model, Xing, Swenson, Weiser, & Hao (2014) found that broad-scale SADs were important drivers of local-scale abundance, arguing that it was thus necessary to discern what the underlying mechanisms of North American tree SADs across broader scales are. The results of our study indicate that temperature is a (perhaps the) key environmental driver governing the form of ENA tree SADs at large meta-community scales, which should thus aid in our understanding of the local-scale variation in tree abundance. This, in turn, suggests that niche factors and environmental filtering are important in structuring ENA tree communities.

## DATA AVAILABILITY

Our analyses were based on publicly available plot-level data produced by the United States Department of Agriculture, Forest Service's Forest Inventory and Analysis Program (<http://fia.fs.fed.us/>).

## REFERENCES

- Allen, A. P., Brown, J. H., & Gillooly, J. F. (2002). Global biodiversity, biochemical kinetics, and the energetic-equivalence rule. *Science*, 297, 1545-1548.
- Allen, A. P., Gillooly, J. F., Savage, V. M., & Brown, J. H. (2006). Kinetic effects of temperature on rates of genetic divergence and speciation. *Proceedings of the National Academy of Sciences*, 103, 9130-9135.

- Anderegg, W. R. L., Flint, A., Huang, C.-y., Flint, L., Berry, J. A., Davis, Frank W., . . . Field, C. B. (2015). Tree mortality predicted from drought-induced vascular damage. *Nature Geoscience*, 8, 367.
- Antão, L. H., Connolly, S. R., Magurran, A. E., Soares, A., & Dornelas, M. (2017). Prevalence of multimodal species abundance distributions is linked to spatial and taxonomic breadth. *Global Ecology and Biogeography*, 26, 203-215.
- Arellano, G., Umaña, M. N., Macía, M. J., Loza, M. I., Fuentes, A., Cala, V., & Jørgensen, P. M. (2017). The role of niche overlap, environmental heterogeneity, landscape roughness and productivity in shaping species abundance distributions along the Amazon–Andes gradient. *Global Ecology and Biogeography*, 26, 191-202.
- Bartoń, K. (2012). *MuMIn: multi-model inference* (R Package version 1.2). Retrieved from <https://cran.r-project.org/web/packages/MuMIn/index.html>
- Bazzaz, F. A. (1975). Plant species diversity in old-field successional ecosystems in Southern Illinois. *Ecology*, 56, 485-488.
- Bivand, R. (2017). *spdep: spatial dependence: weighting schemes, statistics and models* (R Package version 0.6-13). Retrieved from <https://cran.r-project.org/web/packages/spdep/index.html>
- Brown, J. H., Gillooly, J. F., Allen, A. P., Savage, V. M., & West, G. B. (2004). Toward a metabolic theory of ecology. *Ecology*, 85, 1771-1789.
- Burnham, K. P., & Anderson, D. R. (2002). *Model selection and multi-model inference: a practical information-theoretic approach* (2nd ed.). New-York: Springer.
- Burnham, K.P., & Anderson, D.R. (2004). Multimodel inference: understanding AIC and BIC in model selection. *Sociological Methods & Research*, 33, 261-304.
- Currie, D. J., Mittelbach, G. G., Cornell, H. V., Field, R., Guégan, J.-F., Hawkins, B. A., . . . Turner, J. R. G. (2004). Predictions and tests of climate-based hypotheses of broad-scale variation in taxonomic richness. *Ecology Letters*, 7, 1121-1134.
- Currie, D. J., & Paquin, V. (1987). Large-scale biogeographical patterns of species richness of trees. *Nature*, 329, 326-327.
- Dornelas, M., & Connolly, S. R. (2008). Multiple modes in a coral species abundance distribution. *Ecology Letters*, 11, 1008-1016.
- Dornelas, M., Soykan, C. U., & Ugland, K. I. (2011). Biodiversity and disturbance. In A. E. Magurran & B. J. McGill (Eds.), *Biological diversity: frontiers in measurement and assessment* (pp. 237-251). Oxford: Oxford University Press.
- Fick, S. E., & Hijmans, R. J. (2017). WorldClim 2: new 1-km spatial resolution climate surfaces for global land areas. *International Journal of Climatology*, 37, 4302-4315.
- Field, R., Hawkins, B. A., Cornell, H. V., Currie, D. J., Diniz-Filho, J. A. F., Guégan, J.-F., . . . Turner, J. R. G. (2009). Spatial species-richness gradients across scales: a meta-analysis. *Journal of Biogeography*, 36, 132-147.

- Fisher, R. A., Corbet, A. S., & Williams, C. B. (1943). The relation between the number of species and the number of individuals in a random sample of an animal population. *Journal of Animal Ecology*, 12, 42-58.
- Gaston, K. J., & Blackburn, T. M. (2000). *Patterns and process in macroecology*. Oxford: Blackwell Science.
- Giam, X., & Olden, J. D. (2016). Quantifying variable importance in a multimodel inference framework. *Methods in Ecology and Evolution*, 7, 388-397.
- Harte, J. (2011). *Maximum entropy and ecology: a theory of abundance, distribution, and energetics* (Vol. Oxford): Oxford University Press.
- Hawkins, B. A., Field, R., Cornell, H. V., Currie, D. J., Guégan, J.-F., Kaufman, D. M., . . . Turner, J. R. G. (2003). Energy, water, and broad-scale geographic patterns of species richness. *Ecology*, 84, 3105-3117.
- Hijmans, R. J. (2017). *raster: geographic data analysis and modeling* (R Package version 2.6). Retrieved from <https://cran.r-project.org/web/packages/raster/index.html>
- Kubota, Y., Kusumoto, B., Shiono, T., Ulrich, W., & Jabot, F. (2015). Non-neutrality in forest communities: evolutionary and ecological determinants of tree species abundance distributions. *Oikos*, 125, 237-244.
- Locey, K. J., & White, E. P. (2013). How species richness and total abundance constrain the distribution of abundance. *Ecology Letters*, 16, 1177-1185.
- Mac Nally, R., Duncan, R. P., Thomson, J. R., & Yen, J. D. L. (2018). Model selection using information criteria, but is the 'best' model any good? *Journal of Applied Ecology*, 55, 1441-1444.
- MacArthur, R. H. (1960). On the relative abundance of species. *American Naturalist*, 94, 25-36.
- MacArthur, R. H. (1972). *Geographical ecology*. Princeton: Princeton University Press.
- Magurran, A. E., & Henderson, P. A. (2003). Explaining the excess of rare species in natural species abundance distributions. *Nature*, 422, 714-716.
- Matthews, T. J., Borregaard, M. K., Gillespie, C. S., Rigal, F., Ugland, K. I., Krüger, R. F., Marques, R., Sadler, J. P., Borges, P. A., Kubota, Y., & Whittaker, R. J. (2018). Extension of the gambin model to multimodal species abundance distributions. *Methods in Ecology and Evolution*, doi:10.1111/2041-210X.13122
- Matthews, T. J., Borges, P. A. V., de Azevedo, E. B., & Whittaker, R. J. (2017). A biogeographical perspective on species abundance distributions: recent advances and opportunities for future research. *Journal of Biogeography*, 44, 1705-1710
- Matthews, T. J., Borregaard, M. K., Ugland, K. I., Borges, P. A. V., Rigal, F., Cardoso, P., & Whittaker, R. J. (2014). The gambin model provides a superior fit to species abundance distributions with a single free parameter: evidence, implementation and interpretation. *Ecography*, 37, 1002-1011.

- Matthews, T. J., & Whittaker, R. J. (2015). On the species abundance distribution in applied ecology and biodiversity management. *Journal of Applied Ecology*, 52, 443-454.
- May, R. M. (1975). Patterns of species abundance and diversity. In M. L. Cody & J. M. Diamond (Eds.), *Ecology and evolution of communities* (pp. 81-120). Cambridge, MA: Harvard University Press.
- McGill, B. J. (2011). Species abundance distributions. In A. E. Magurran & B. J. McGill (Eds.), *Biological diversity: frontiers in measurement and assessment* (pp. 105-122). Oxford: Oxford University Press.
- McGill, B. J., Etienne, R. S., Gray, J. S., Alonso, D., Anderson, M. J., Benecha, H. K., . . . White, E. P. (2007). Species abundance distributions: moving beyond single prediction theories to integration within an ecological framework. *Ecology Letters*, 10, 995-1015.
- O'Connell, B. M., Conkling, B. L., Wilson, A. M., Burrill, E. A., Turner, J. A., Pugh, S. A., . . . Menlove, J. (2017). *The forest inventory and analysis database: database description and user guide for phase 2* (version 7.0). Retrieved from [https://www.fia.fs.fed.us/library/database-documentation/current/ver70/FIADB%20User%20Guide%20P2\\_7-0\\_ntc.final.pdf](https://www.fia.fs.fed.us/library/database-documentation/current/ver70/FIADB%20User%20Guide%20P2_7-0_ntc.final.pdf)
- Preston, F. W. (1948). The commonness, and rarity, of species. *Ecology*, 29, 254-283.
- R Core Team. (2017). *R: A language and environment for statistical computing* (Version 3.4.3). Vienna, Austria: R foundation for statistical computing.
- Rosenzweig, M. L. (1995). *Species diversity in space and time*. Cambridge: Cambridge University Press.
- Ugland, K. I., Lambshead, P. J. D., McGill, B., Gray, J. S., O'Dea, N., Ladle, R. J., & Whittaker, R. J. (2007). Modelling dimensionality in species abundance distributions: description and evaluation of the Gambin model. *Evolutionary Ecology Research*, 9, 313-324.
- Ulrich, W., Nakadai, R., Matthews, T.J. & Kubota, Y. (2018) The two-parameter Weibull distribution as a universal tool to model the variation in species relative abundances. *Ecological Complexity*, 36, 110-116.
- Ulrich, W., Kusumoto, B., Shiono, T., & Kubota, Y. (2016). Climatic and geographic correlates of global forest tree species–abundance distributions and community evenness. *Journal of Vegetation Science*, 27, 295-305.
- Ulrich, W., Olrik, M., & Ugland, K. I. (2010). A meta-analysis of species–abundance distributions. *Oikos*, 119, 1149-1155.
- Vergnon, R., van Nes, E. H., & Scheffer, M. (2012). Emergent neutrality leads to multimodal species abundance distributions. *Nature Communications*, 3, 663.
- Volkov, I., Banavar, J. R., Hubbell, S. P., & Maritan, A. (2003). Neutral theory and relative species abundance in ecology. *Nature*, 424, 1035-1037.



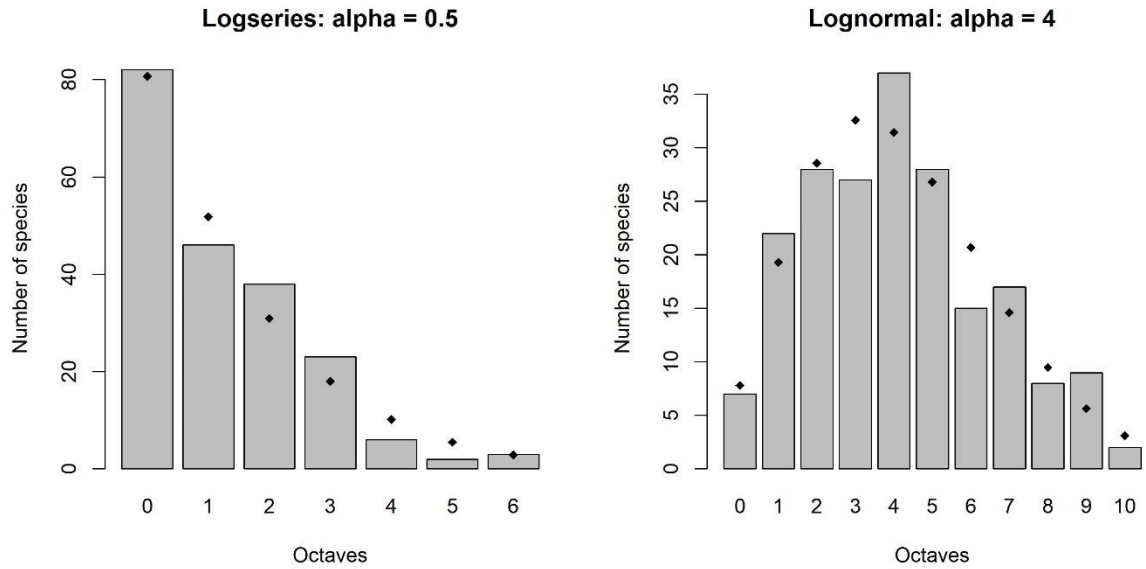
- White, E. P., Thibault, K. M., & Xiao, X. (2012). Characterizing species abundance distributions across taxa and ecosystems using a simple maximum entropy model. *Ecology*, 93, 1772-1778.
- Whittaker, R. J., Willis, K. J., & Field, R. (2003). Climatic–energetic explanations of diversity: a macroscopic perspective. In T. M. Blackburn & K. J. Gaston (Eds.), *Macroecology: concepts and consequences* (pp. 107-129). Malden, USA: Blackwell.
- Wiens, J. J., Ackerly, D. D., Allen, A. P., Anacker, B. L., Buckley, L. B., Cornell, H. V., . . . Stephens, P. R. (2010). Niche conservatism as an emerging principle in ecology and conservation biology. *Ecology Letters*, 13, 1310-1324.
- Xing, D., Swenson, N. G., Weiser, M. D., & Hao, Z. (2014). Determinants of species abundance for eastern North American trees. *Global Ecology and Biogeography*, 23, 903-911.

**TABLE 1.** Spatial error model selection results. The response variable in all models was the alpha parameter of the gambin species abundance distribution model (log transformed). The three predictors (temperature, precipitation and species richness) were standardised to have a mean of zero and standard deviation of one. The data were pooled samples (N = 737) of North American tree monitoring plots. The abundance data of each sample were standardised to ensure all samples contained 500 individuals. For each model, the variable coefficient estimate is given with the standard error in parentheses. The AIC,  $\Delta$ AIC, and the Z-value of each model are also provided. \*indicates a significant Z-value at the  $p \leq 0.001$  level.

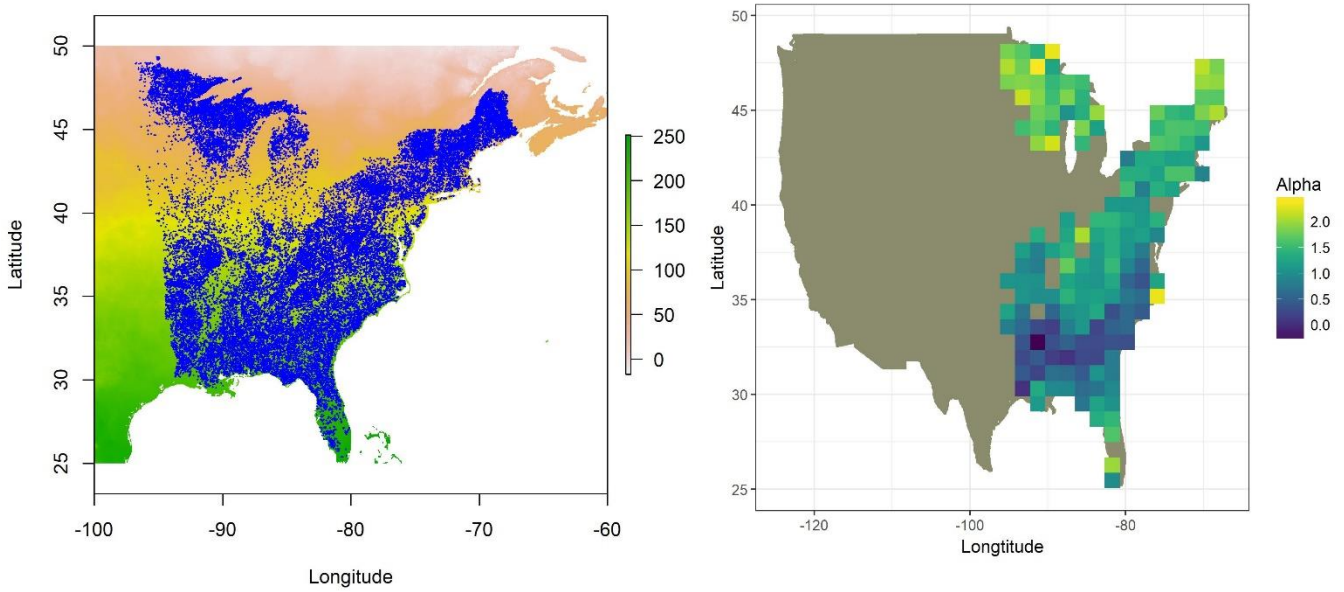
Rank	Temperature	Precipitation	Species richness	AIC	$\Delta$ AIC	Z-value
1	-0.39 (0.03)	-	-0.12 (0.02)	643.4	0.0	14.64*
2	-0.36 (0.04)	-0.04 (0.04)	-0.12 (0.02)	644.8	1.4	14.85*
3	-	-0.27 (0.04)	-0.14 (0.02)	694.6	51.2	22.80*
4	-	-	-0.15 (0.02)	730.0	86.6	29.57*
5	-	-	-	775.8	132.5	32.96*

**TABLE 2.** Binomial GLM model selection results. Models were compared using AIC. All models with a  $\Delta\text{AIC} \leq 2$  are shown. The response variable in all models was a binary variable describing whether or not a two-component gambin model provided a better fit than a one-component gambin model. The five predictors were: temperature (Temp.), precipitation (Precip.), number of individuals in a sample (N), a spatial autocovariate (AutCov) and species richness (SR). All predictors were standardised to have a mean of zero and standard deviation of one. The data were pooled samples of North American tree monitoring plots ( $n = 653$ ). For each model, the variable coefficient estimate is given with the standard error in parentheses. The AIC and  $\Delta\text{AIC}$  of each model are also provided.

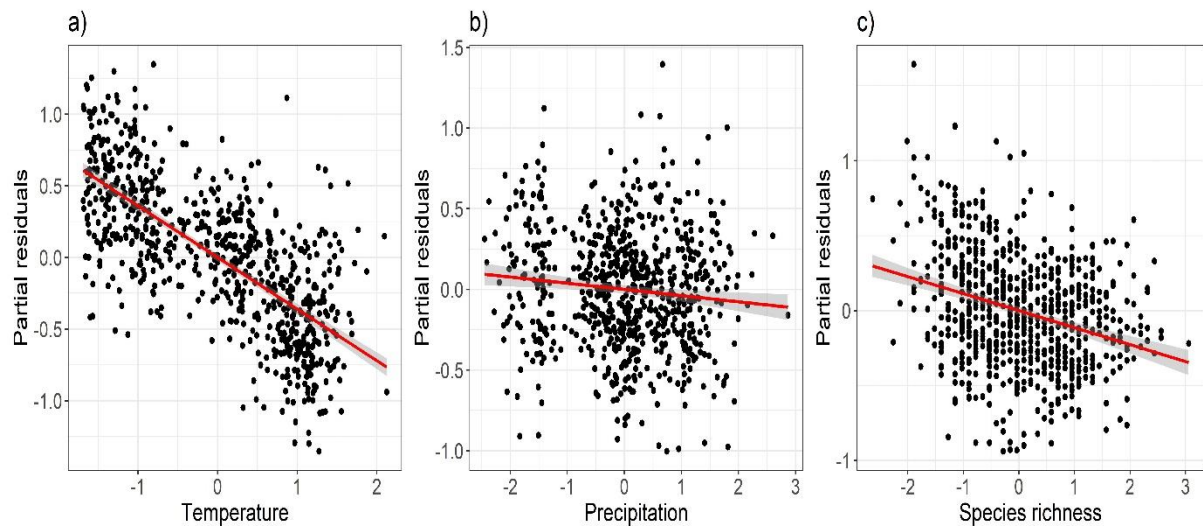
Rank	AutCov	N	Precip.	SR	Temp.	AIC	$\Delta\text{AIC}$
1	-0.21 (0.12)	-0.22 (0.14)	-	0.53 (0.17)	-1.05 (0.23)	395.52	0.00
2	-0.22 (0.12)	-	-	0.51 (0.17)	-0.91 (0.20)	396.21	0.69
3	-0.19 (0.12)	-0.24 (0.14)	0.19 (0.21)	0.50 (0.17)	-1.21 (0.29)	396.74	1.22
WoE	1.00	0.60	0.34	0.98	1.00		



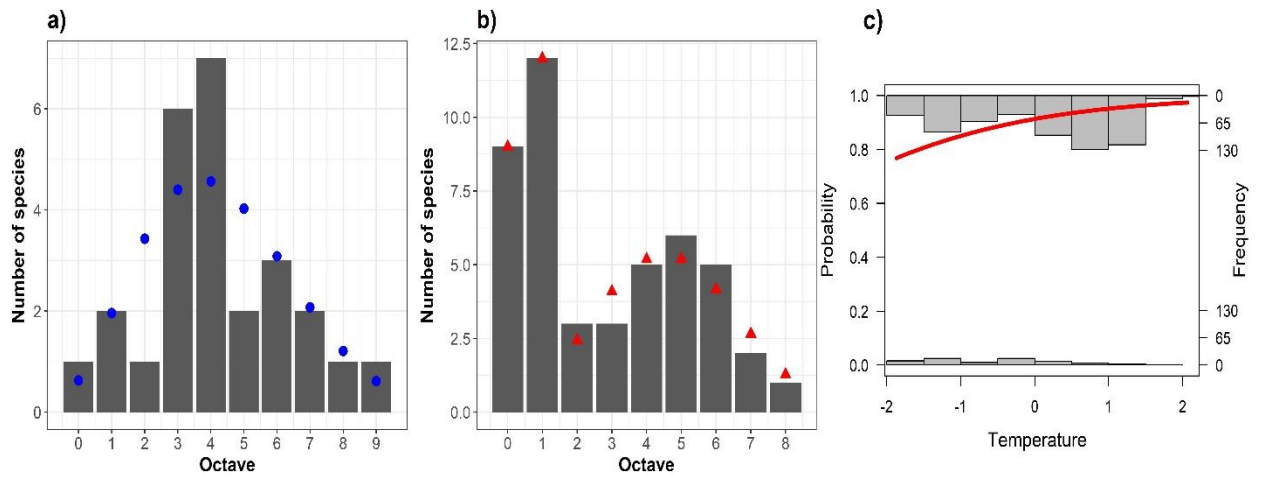
**FIGURE 1.** The two most commonly observed SAD shapes: logseries-like distributions (a), and lognormal-like distributions (b). In both (a) and (b) the gambin model (black circles) has been fitted to the data binned into logarithmic octaves (grey bars). The data were simulated by sampling random values from gambin distributions with alpha parameters of 0.5 (a) and 4 (b); in both plots the number of species was set to 200.



**FIGURE 2.** Left-hand plot: the distribution of 33,282 FIA tree plots (blue dots) across Eastern North America, overlaid on a heat map of temperature values. Temperature data were sourced from the WorldClim database and represents the annual mean temperature at 2.5 min resolution (temperature data are in the form  $^{\circ}\text{C} \times 10$ ). Right-hand plot: a heat map showing spatial variation in the  $\alpha$  parameter (log transformed) of the gambin model; alpha values were grouped into 30 bins and the median value displayed. Lower values of alpha correspond to log-series like SAD shapes, while higher values correspond to more log-normal like SAD shapes (see Fig. 1). The alpha values were generated from fitting the gambin SAD model to tree data from 737 coarse-scale samples, where a sample is a collection of FIA tree monitoring plots within a roughly 44km by 44km grid.



**FIGURE 3.** Partial residual plots showing the effect of temperature (a), precipitation (b) and species richness (c) on the alpha parameter of the gambin SAD model (log transformed), after taking into account the effect of the other independent variables in the global model (i.e. the model containing all three predictors). The red solid line in each plot represents the best fit linear model to the partial residual data. The alpha values were generated from fitting the gambin SAD model to tree data from 737 coarse-scale samples, where a sample is a collection of FIA tree monitoring plots within an approximately 44km by 44km grid.



**FIGURE 4.** An example of a unimodal (a) and bimodal (b) SAD (grey bars), generated using samples of North East American trees, where a sample is a collection of FIA tree plots. In (a) the fit of the one-component gambin model (blue circles), and in (b) the fit of the two-component gambin model (red triangles), are shown. The sample in (a) comprises 26 species and 1902 individuals, and in (b) 46 species and 1456 individuals. In (c) the results of a logistic regression are displayed; the red line represents the curve of the predicted values from the model and the grey bars are the observed data points displayed as histograms. The predictor variable in the model was (standardised) temperature. The response variable in the model was a binary variable indicating whether or not a two-component gambin model provided a better fit than a one-component gambin model to a given sample; we used one minus this value for illustrative purposes, and thus the curve shows an increasing probability of a one-component model providing the best fit with increasing temperature. The data are 653 meta-community scale samples of Eastern North American trees.